



# 基于高斯表示学习的高精度旋转目标检测算法研究

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## 旋转目标检测

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## 问题和挑战

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## 实验分析



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## 实验分析

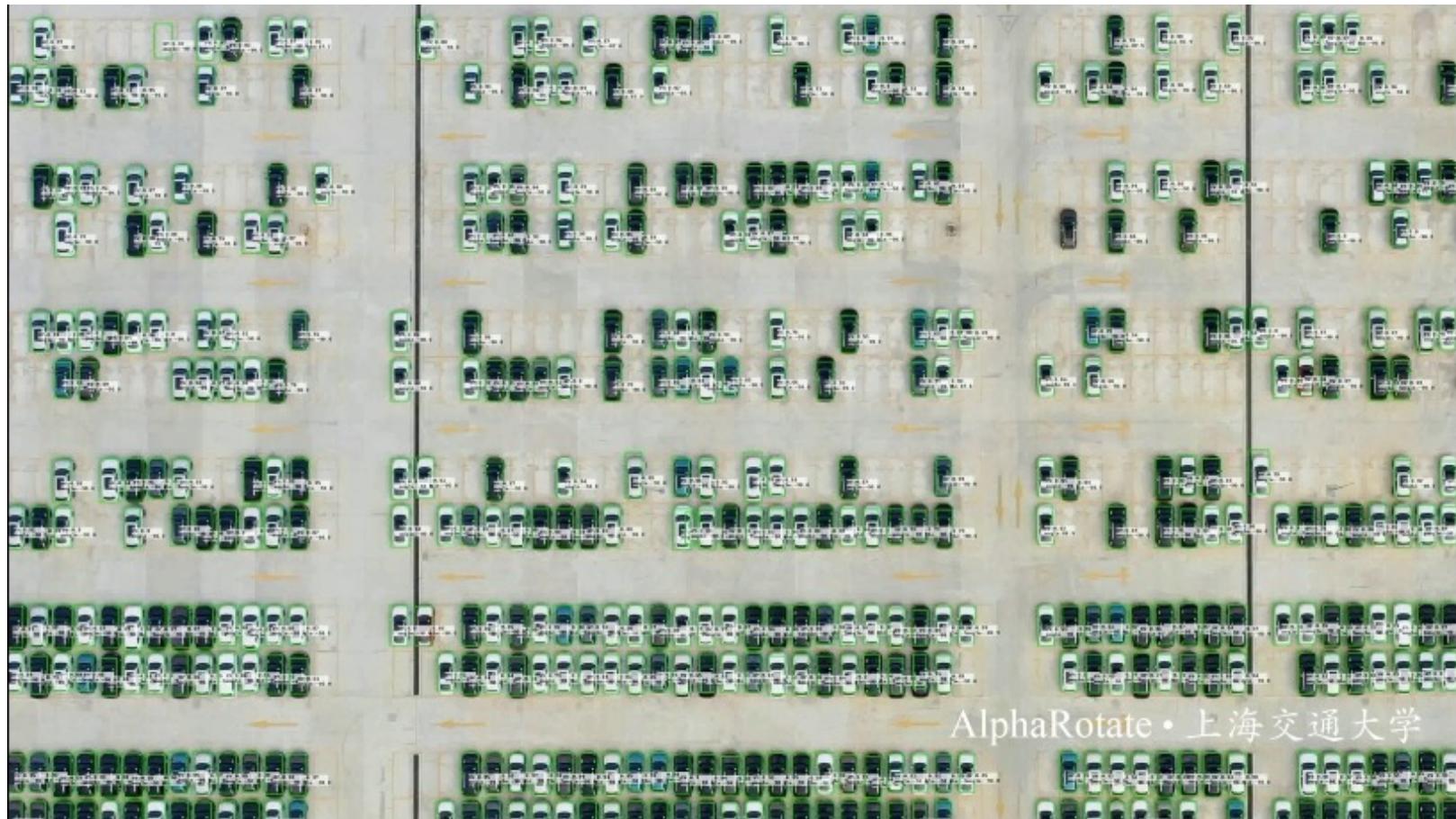




# 旋转目标检测

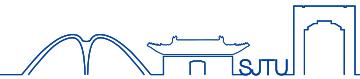


- 预测具有方向的边界框并对目标进行识别



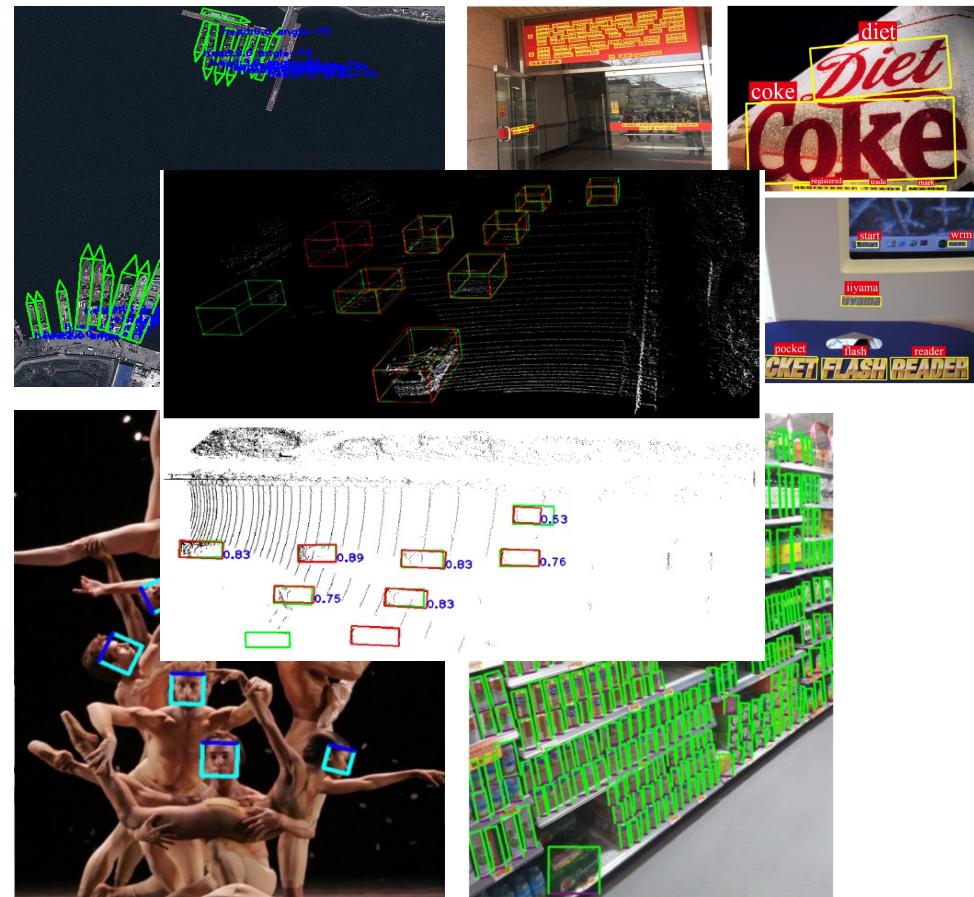


# 旋转目标检测



## 应用场景

- 遥感检测
- 人脸检测
- 零售场景检测
- 场景文字检测
- 3D目标检测



# 旋转目标检测



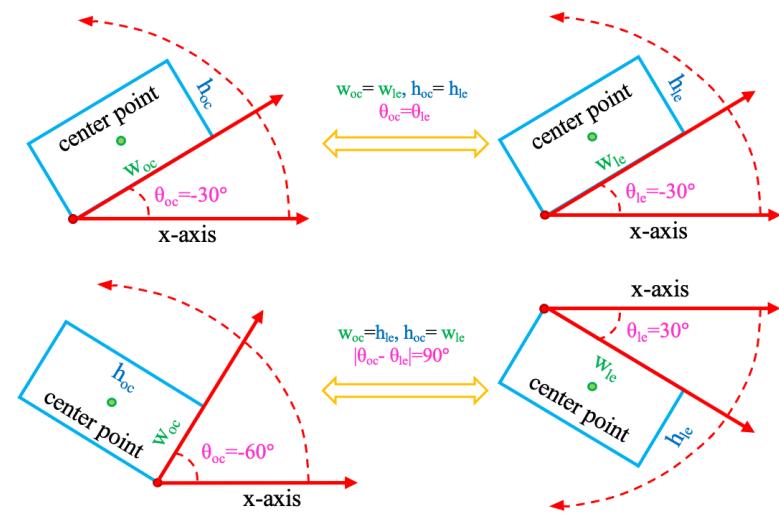
- 旋转框的定义方式：

- OpenCV定义法： $(x, y, w_{oc}, h_{oc}, \theta_{oc})$ ,  $\theta_{oc} \in [-90, 0)$
- 长边定义法： $(x, y, w_{le}, h_{le}, \theta_{le})$ ,  $\theta_{le} \in [-90, 90)$

- 转换关系：

$$D_{le}(w_{le}, h_{le}, \theta_{le}) = \begin{cases} D_{oc}(w_{oc}, h_{oc}, \theta_{oc}), & w_{oc} \geq h_{oc} \\ D_{oc}(h_{oc}, w_{oc}, \theta_{oc} + 90^\circ), & \text{otherwise} \end{cases}$$

$$D_{oc}(w_{oc}, h_{oc}, \theta_{oc}) = \begin{cases} D_{le}(w_{le}, h_{le}, \theta_{le}), & \theta_{le} \in [-90^\circ, 0^\circ) \\ D_{le}(h_{le}, w_{le}, \theta_{le} - 90^\circ), & \text{otherwise} \end{cases}$$





# 旋转目标检测



## ■ 旋转框IoU的计算：

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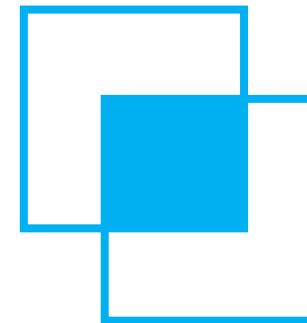
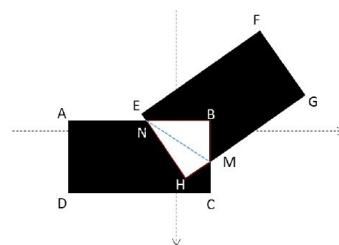
### Algorithm 1 IoU computation

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```
1: Input: Rectangles  $R_1, R_2, \dots, R_N$ 
2:  $\text{IoU}[1, N][1, N] \leftarrow 0$ 
3: for each pair of  $R_i, R_j$  ( $i < j$ ) do
4:   Point set  $PSet \leftarrow \emptyset$ 
5:   Add intersection points of  $R_i$  and  $R_j$  to  $PSet$ 
6:   Add the vertices of  $R_i$  inside  $R_j$  into  $PSet$ 
7:   Add the vertices of  $R_j$  inside  $R_i$  into  $PSet$ 
8:   Sort  $PSet$  to anti-clockwise order
9:   Compute intersection  $I$  of  $PSet$  by triangulation
10:   $\text{IoU}(i, j) \leftarrow (\text{Area}(R_i) + \text{Area}(R_j) - I)/I$ 
11: end for
12: return IoU
```

---

$$\text{IoU} = \frac{\text{Area of Overlap}}{\text{Area of Union}}$$



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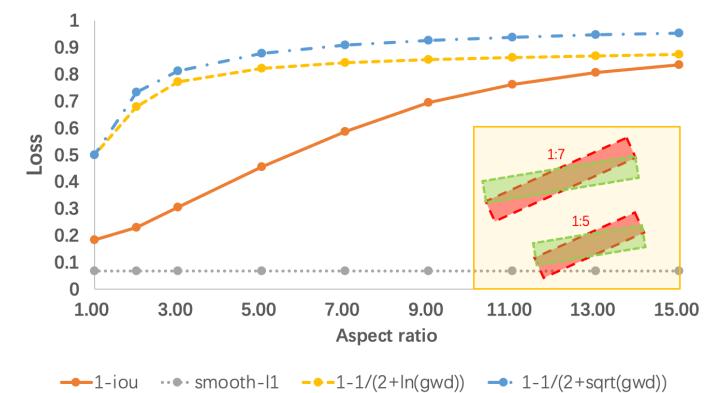
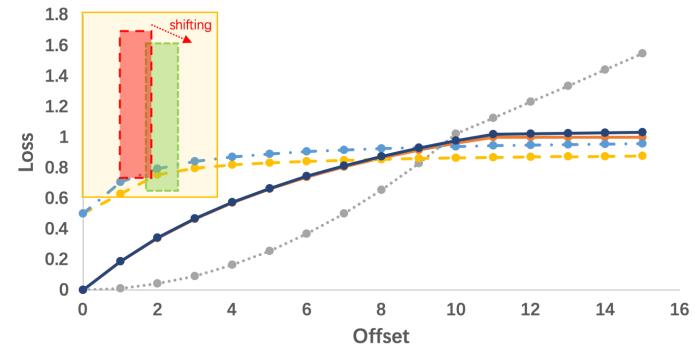
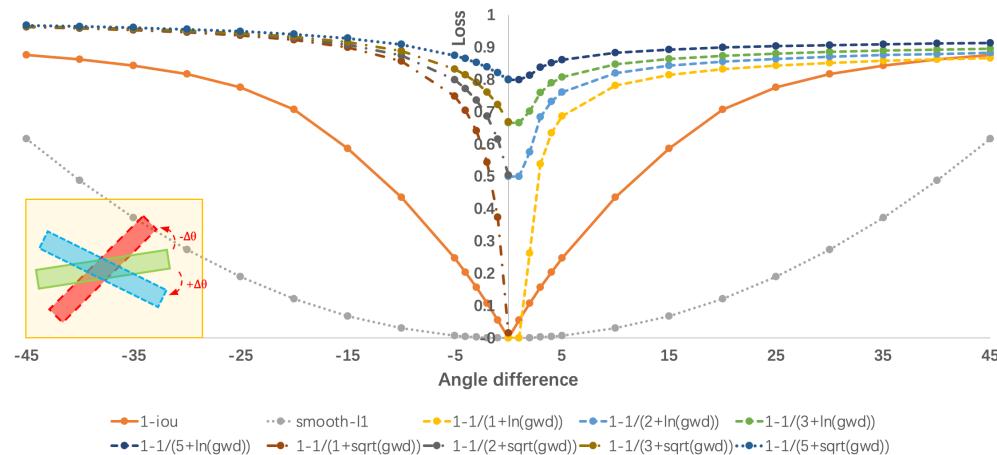
## 实验分析





# 问题和挑战

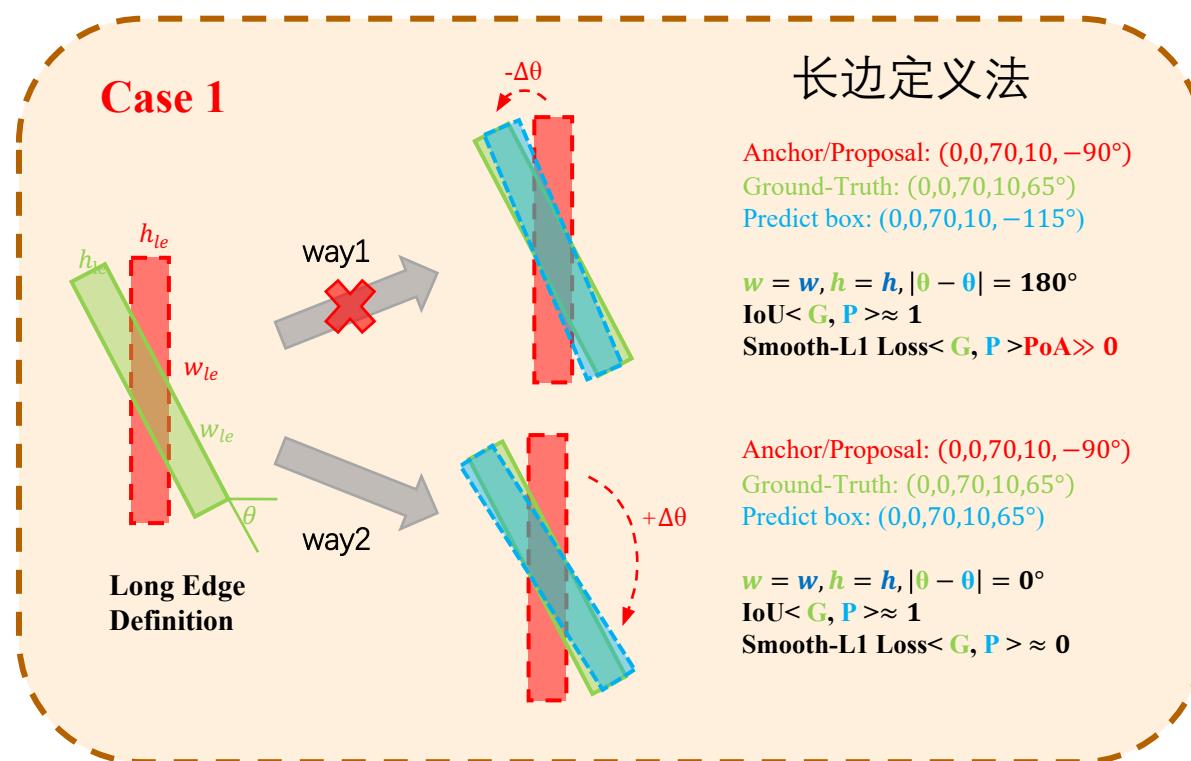
## 评估与损失不一致问题





# 问题和挑战

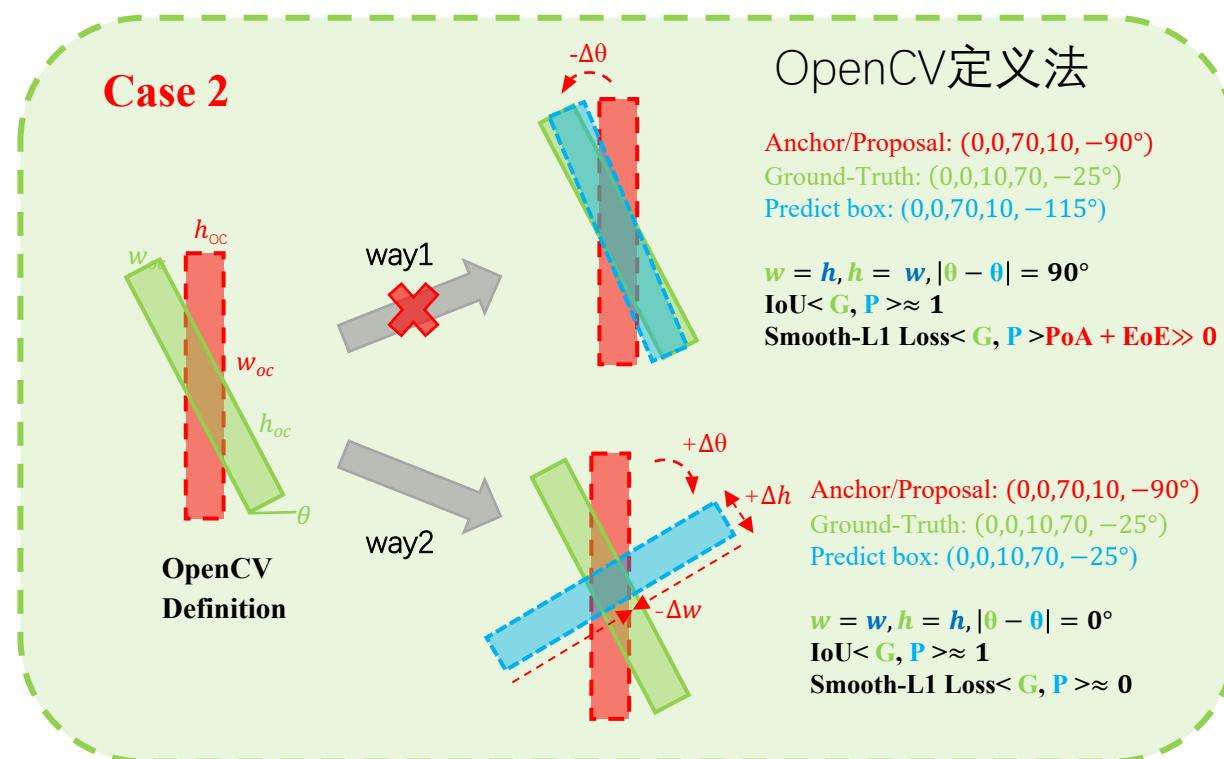
## ▪ 旋转检测中的边界问题





# 问题和挑战

## ▪ 旋转检测中的边界问题





# 问题和挑战

## 类正方形检测问题

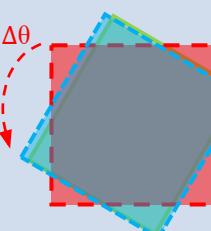
### Case 3

Anchor/Proposal: (0,0,45,44,0°)  
Ground-Truth: (0,0,45,43,−60°)  
Predict box: (0,0,45,44,−60°)

$w \approx w \approx h \approx h, |\theta - 0| = 0^\circ$   
IoU< G, P >≈ 1  
Smooth-L1 Loss< G, P >≈ 0

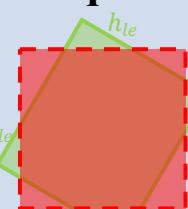
Anchor/Proposal: (0,0,44,45,−90°)  
Ground-Truth: (0,0,45,43,−30°)  
Predict box: (0,0,44,45,−30°)

$w \approx w \approx h \approx h, |\theta - 0| = 0^\circ$   
IoU< G, P >≈ 1  
Smooth-L1 Loss< G, P >≈ 0

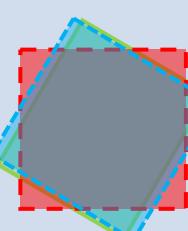


way2

### Square-Like Problem



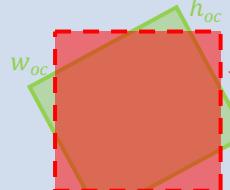
way1



Anchor/Proposal: (0,0,45,44,0°)  
Ground-Truth: (0,0,45,43,−60°)  
Predict box: (0,0,45,44,30°)

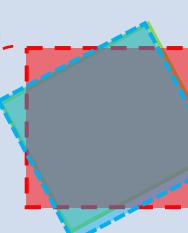
$w \approx w \approx h \approx h, |\theta - 0| = 90^\circ$   
IoU< G, P >≈ 1  
Smooth-L1 Loss< G, P >≈ 0

### Long Edge Definition



way1

### OpenCV Definition



Anchor/Proposal: (0,0,44,45,−90°)  
Ground-Truth: (0,0,45,43,−30°)  
Predict box: (0,0,44,45,−120°)

$w \approx w \approx h \approx h, |\theta - 0| = 90^\circ$   
IoU< G, P >≈ 1  
Smooth-L1 Loss< G, P >= PoA ≫ 0

长宽比越小，IoU对角度越不敏感

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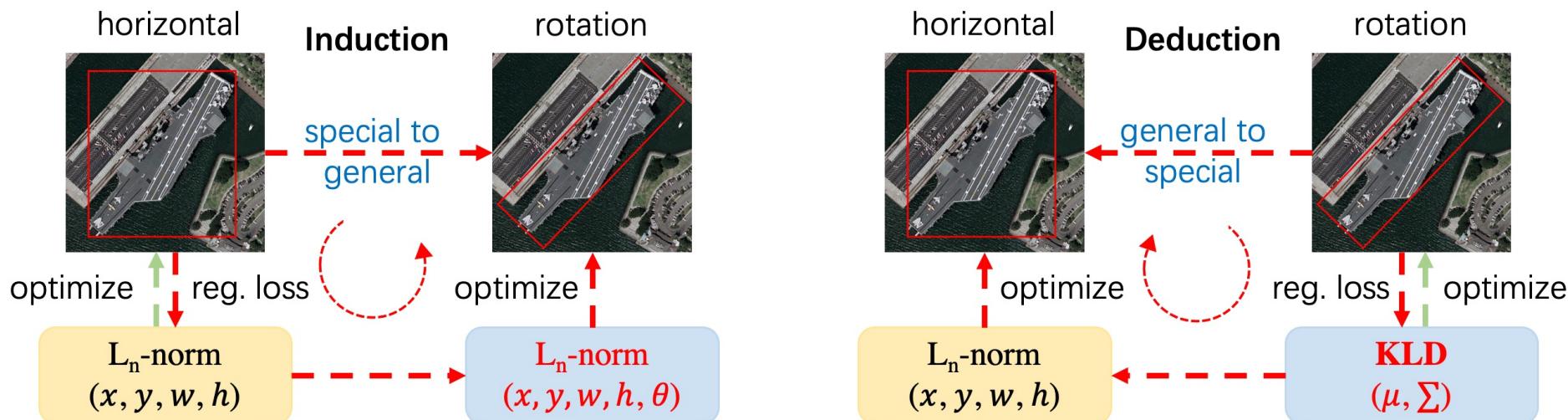
## 实验分析





# 解决方法

- 旋转检测器的两种设计范式
  - 归纳范式
  - 演绎范式



X. Yang, et al. "Rethinking Rotated Object Detection with Gaussian Wasserstein Distance Loss." In ICML 2021.

X. Yang, et al. "Learning High-Precision Bounding Box for Rotated Object Detection via Kullback-Leibler Divergence." In NeurIPS 2021.

# 解决方法



## ▪ 归纳范式

- 对于常见的通用检测模型（水平框检测），模型通常是通过回归四个偏移量的形式来进行框位置和大小的预测：

$$t_x^p = \frac{x_p - x_a}{w_a}, t_y^p = \frac{y_p - y_a}{h_a}, t_w^p = \ln\left(\frac{w_p}{w_a}\right), t_h^p = \ln\left(\frac{h_p}{h_a}\right)$$

来匹配实际的偏移量：

$$t_x^t = \frac{x_t - x_a}{w_a}, t_y^t = \frac{y_t - y_a}{h_a}, t_w^t = \ln\left(\frac{w_t}{w_a}\right), t_h^t = \ln\left(\frac{h_t}{h_a}\right)$$

- 借鉴于此，目前绝大多数的旋转目标检测在上面的基础上加上了角度参数的回归：

$$t_\theta^p = f(\theta_p - \theta_a), t_\theta^t = f(\theta_t - \theta_a)$$



# 解决方法

- 归纳范式

- 然后回归损失也常采用 $L_n$ -norm：

$$L_{reg} = l_n\text{-norm}(\Delta t_x, \Delta t_y, \Delta t_w, \Delta t_h, \Delta t_\theta)$$

where  $\Delta t_x = t_x^p - t_x^t = \frac{\Delta x}{w_a}$ ,  $\Delta t_y = t_y^p - t_y^t = \frac{\Delta y}{h_a}$ ,  $\Delta t_w = t_w^p - t_w^t = \ln(w_p/w_t)$ ,  $\Delta t_h = t_h^p - t_h^t = \ln(h_p/h_t)$ , and  $\Delta t_\theta = t_\theta^p - t_\theta^t = \Delta\theta$ .

- 五个参数独立优化使得我们需要根据不同的数据集特点进行权重的调整，比如大长宽比目标可能需要着重关注角度参数，小目标则需要关注中心点参数，因此这些参数的轻微偏移都会造成这些目标预测精准度（IoU）的急剧下降。



# 解决方法

## ▪ 演绎范式

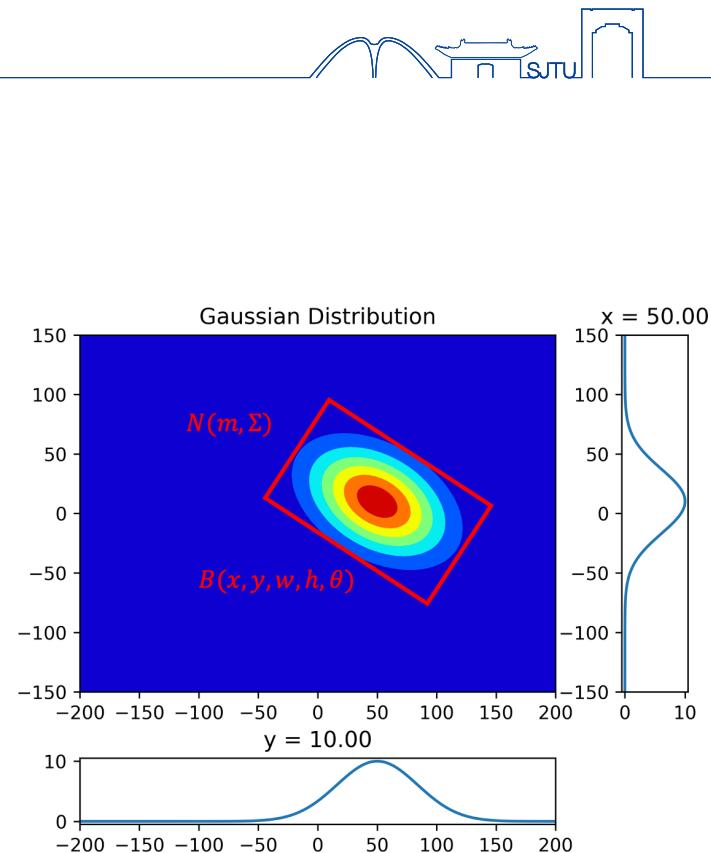
- 要求 1：与 IoU 度量高度一致
- 要求 2：易实现、可微分允许直接学习
- 要求 3：在角度边界情况下平滑

$$\begin{aligned}\Sigma^{1/2} &= \mathbf{R} \mathbf{S} \mathbf{R}^\top \\ &= \begin{pmatrix} \cos \theta & -\sin \theta \\ \sin \theta & \cos \theta \end{pmatrix} \begin{pmatrix} \frac{w}{2} & 0 \\ 0 & \frac{h}{2} \end{pmatrix} \begin{pmatrix} \cos \theta & \sin \theta \\ -\sin \theta & \cos \theta \end{pmatrix} \\ &= \begin{pmatrix} \frac{w}{2} \cos^2 \theta + \frac{h}{2} \sin^2 \theta & \frac{w-h}{2} \cos \theta \sin \theta \\ \frac{w-h}{2} \cos \theta \sin \theta & \frac{w}{2} \sin^2 \theta + \frac{h}{2} \cos^2 \theta \end{pmatrix} \\ \mathbf{m} &= (x, y)^\top\end{aligned}$$

**Property 1:**  $\Sigma^{1/2}(w, h, \theta) = \Sigma^{1/2}(h, w, \theta - \frac{\pi}{2})$ ;

**Property 2:**  $\Sigma^{1/2}(w, h, \theta) = \Sigma^{1/2}(w, h, \theta - \pi)$ ;

**Property 3:**  $\Sigma^{1/2}(w, h, \theta) \approx \Sigma^{1/2}(w, h, \theta - \frac{\pi}{2})$ , if  $w \approx h$ .





# 解决方法

- Wasserstein Distance

- 通用公式：

$$\mathbf{D}_w(\mathcal{N}_p, \mathcal{N}_t)^2 = \underbrace{\|\boldsymbol{\mu}_p - \boldsymbol{\mu}_t\|_2^2}_{\text{center distance}} + \underbrace{\text{Tr}(\boldsymbol{\Sigma}_p + \boldsymbol{\Sigma}_t - 2(\boldsymbol{\Sigma}_p^{1/2} \boldsymbol{\Sigma}_t \boldsymbol{\Sigma}_p^{1/2})^{1/2})}_{\text{coupling terms about } h_p, w_p \text{ and } \theta_p}$$

- 水平特殊情况：

$$\begin{aligned}\mathbf{D}_w^h(\mathcal{N}_p, \mathcal{N}_t)^2 &= \|\boldsymbol{\mu}_p - \boldsymbol{\mu}_t\|_2^2 + \|\boldsymbol{\Sigma}_p^{1/2} - \boldsymbol{\Sigma}_t^{1/2}\|_F^2 \\ &= (x_p - x_t)^2 + (y_p - y_t)^2 + ((w_p - w_t)^2 + (h_p - h_t)^2) / 4 \\ &= l_2\text{-norm}(\Delta x, \Delta y, \Delta w/2, \Delta h/2)\end{aligned}$$



# 解决方法

- Kullback-Leibler Divergence

- 通用公式：

或

$$\mathbf{D}_{kl}(\mathcal{N}_p || \mathcal{N}_t) = \underbrace{\frac{1}{2}(\boldsymbol{\mu}_p - \boldsymbol{\mu}_t)^\top \boldsymbol{\Sigma}_t^{-1} (\boldsymbol{\mu}_p - \boldsymbol{\mu}_t)}_{\text{term about } x_p \text{ and } y_p} + \underbrace{\frac{1}{2} \mathbf{Tr}(\boldsymbol{\Sigma}_t^{-1} \boldsymbol{\Sigma}_p) + \frac{1}{2} \ln \frac{|\boldsymbol{\Sigma}_t|}{|\boldsymbol{\Sigma}_p|}}_{\text{coupling terms about } h_p, w_p \text{ and } \theta_p} - 1$$

$$\mathbf{D}_{kl}(\mathcal{N}_t || \mathcal{N}_p) = \underbrace{\frac{1}{2}(\boldsymbol{\mu}_p - \boldsymbol{\mu}_t)^\top \boldsymbol{\Sigma}_p^{-1} (\boldsymbol{\mu}_p - \boldsymbol{\mu}_t) + \frac{1}{2} \mathbf{Tr}(\boldsymbol{\Sigma}_p^{-1} \boldsymbol{\Sigma}_t) + \frac{1}{2} \ln \frac{|\boldsymbol{\Sigma}_p|}{|\boldsymbol{\Sigma}_t|}}_{\text{chain coupling of all parameters}} - 1$$

- 水平特殊情况：

$$\begin{aligned} \mathbf{D}_{kl}^h(\mathcal{N}_p || \mathcal{N}_t) &= \frac{1}{2} \left( \frac{w_p^2}{w_t^2} + \frac{h_p^2}{h_t^2} + \frac{4\Delta^2 x}{w_t^2} + \frac{4\Delta^2 y}{h_t^2} + \ln \frac{w_t^2}{w_p^2} + \ln \frac{h_t^2}{h_p^2} - 2 \right) \\ &= 2l_2\text{-norm}(\Delta t_x, \Delta t_y) + l_1\text{-norm}(\Delta t_w, \Delta t_h) + \frac{1}{2} l_2\text{-norm}\left(\frac{1}{\Delta t_w}, \frac{1}{\Delta t_h}\right) - 1 \end{aligned}$$



# 解决方法

- 高精度分析 (KLD>GWD>smooth L1) :

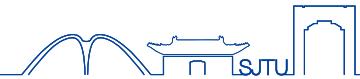
- KLD主要三项的具体表达式：

$$(\boldsymbol{\mu}_p - \boldsymbol{\mu}_t)^\top \boldsymbol{\Sigma}_t^{-1} (\boldsymbol{\mu}_p - \boldsymbol{\mu}_t) = \frac{4(\Delta x \cos \theta_t + \Delta y \sin \theta_t)^2}{w_t^2} + \frac{4(\Delta y \cos \theta_t - \Delta x \sin \theta_t)^2}{h_t^2}$$

$$\text{Tr}(\boldsymbol{\Sigma}_t^{-1} \boldsymbol{\Sigma}_p) = \frac{h_p^2}{w_t^2} \sin^2 \Delta\theta + \frac{w_p^2}{h_t^2} \sin^2 \Delta\theta + \frac{h_p^2}{h_t^2} \cos^2 \Delta\theta + \frac{w_p^2}{w_t^2} \cos^2 \Delta\theta$$

$$\ln \frac{|\boldsymbol{\Sigma}_t|}{|\boldsymbol{\Sigma}_p|} = \ln \frac{h_t^2}{h_p^2} + \ln \frac{w_t^2}{w_p^2}$$

其中  $\Delta x = x_p - x_t, \Delta y = y_p - y_t, \Delta\theta = \theta_p - \theta_t$  。



# 解决方法

- 高精度分析 (KLD>GWD>smooth L1) :

- 不失一般性，我们令  $\theta_t = 0$ ，对KLD的 $\mu_p$ 求导数：

$$\frac{\partial \mathbf{D}_{kl}(\mu_p)}{\partial \mu_p} = \left( \frac{4}{w_t^2} \Delta x, \frac{4}{h_t^2} \Delta y \right)^\top$$

- 当 $\theta_t \neq 0$ 时，目标的偏移量（ $\Delta x$ 和 $\Delta y$ ）的梯度会根据角度进行动态调整以提供更好的优化。相比之下，GWD和 $L_2$ 关于偏移量的梯度分别是：

$$\frac{\partial \mathbf{D}_w(\mu_p)}{\partial \mu_p} = (2\Delta x, 2\Delta y)^\top \quad \frac{\partial L_2(\mu_p)}{\partial \mu_p} = \left( \frac{2}{w_a^2} \Delta x, \frac{2}{h_a^2} \Delta y \right)^\top$$



# 解决方法

- 高精度分析 (KLD>GWD>smooth L1) :

- 对KLD的 $h_p$ 和 $w_p$ 求导数：

$$\frac{\partial \mathbf{D}_{kl}(\Sigma_p)}{\partial \ln h_p} = \frac{h_p^2}{h_t^2} \cos^2 \Delta\theta + \frac{h_p^2}{w_t^2} \sin^2 \Delta\theta - 1, \quad \frac{\partial \mathbf{D}_{kl}(\Sigma_p)}{\partial \ln w_p} = \frac{w_p^2}{w_t^2} \cos^2 \Delta\theta + \frac{w_p^2}{h_t^2} \sin^2 \Delta\theta - 1$$

我们可以看到，两边 $h_p$ 和 $w_p$ 梯度和角度差 $\Delta\theta$ 有关。当 $\Delta\theta = 0$ 时：

$$\frac{\partial \mathbf{D}_{kl}(\Sigma_p)}{\partial \ln h_p} = \frac{h_p^2}{h_t^2} - 1, \quad \frac{\partial \mathbf{D}_{kl}(\Sigma_p)}{\partial \ln w_p} = \frac{w_p^2}{w_t^2} - 1$$

这意味着较小的目标尺度会导致其匹配到更大的损失。这是符合认知的，因为较小的边需要更高的匹配精度。



# 解决方法

- 高精度分析 (KLD>GWD>smooth L1) :

- 对 $\theta$ 求导数：

$$\frac{\partial \mathbf{D}_{kl}(\Sigma_p)}{\partial \theta_p} = \left( \frac{h_p^2 - w_p^2}{w_t^2} + \frac{w_p^2 - h_p^2}{h_t^2} \right) \sin 2\Delta\theta$$

- 角度差 $\Delta\theta$ 的优化又和两边 $h_p$ 和 $w_p$ 有关。当 $h_p = h_t$ ,  $w_p = w_t$ 时：

$$\frac{\partial \mathbf{D}_{kl}(\Sigma_p)}{\partial \theta_p} = \left( \frac{h_t^2}{w_t^2} + \frac{w_t^2}{h_t^2} - 2 \right) \sin 2\Delta\theta \geq \sin 2\Delta\theta$$

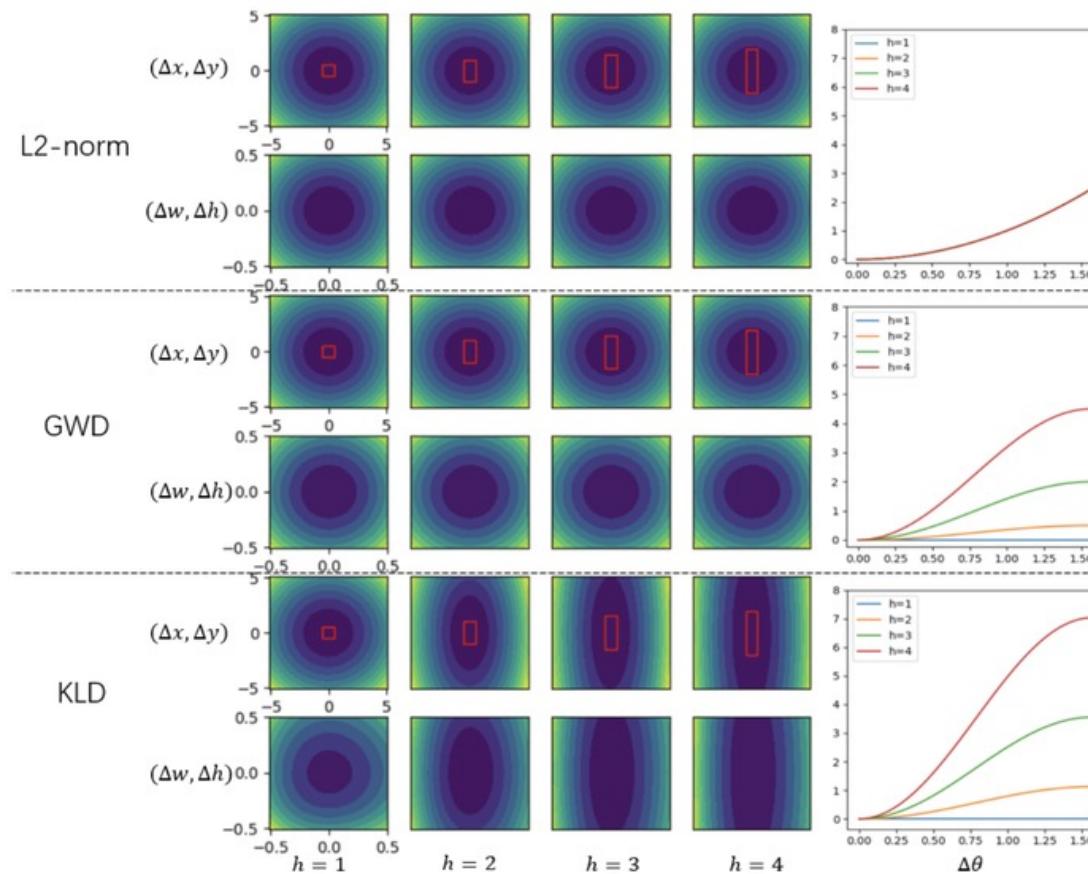
- 当目标长宽比慢慢变大的时候，整个式子的值就会变大，也就是意味着对角度优化更加看重。这个优化机制是非常好的，我们知道对于长宽比越大的目标来说，它受角度差的影响就越大，IoU会产生急剧下降。



# 解决方法



- 高精度分析 (KLD>GWD>smooth L1) :

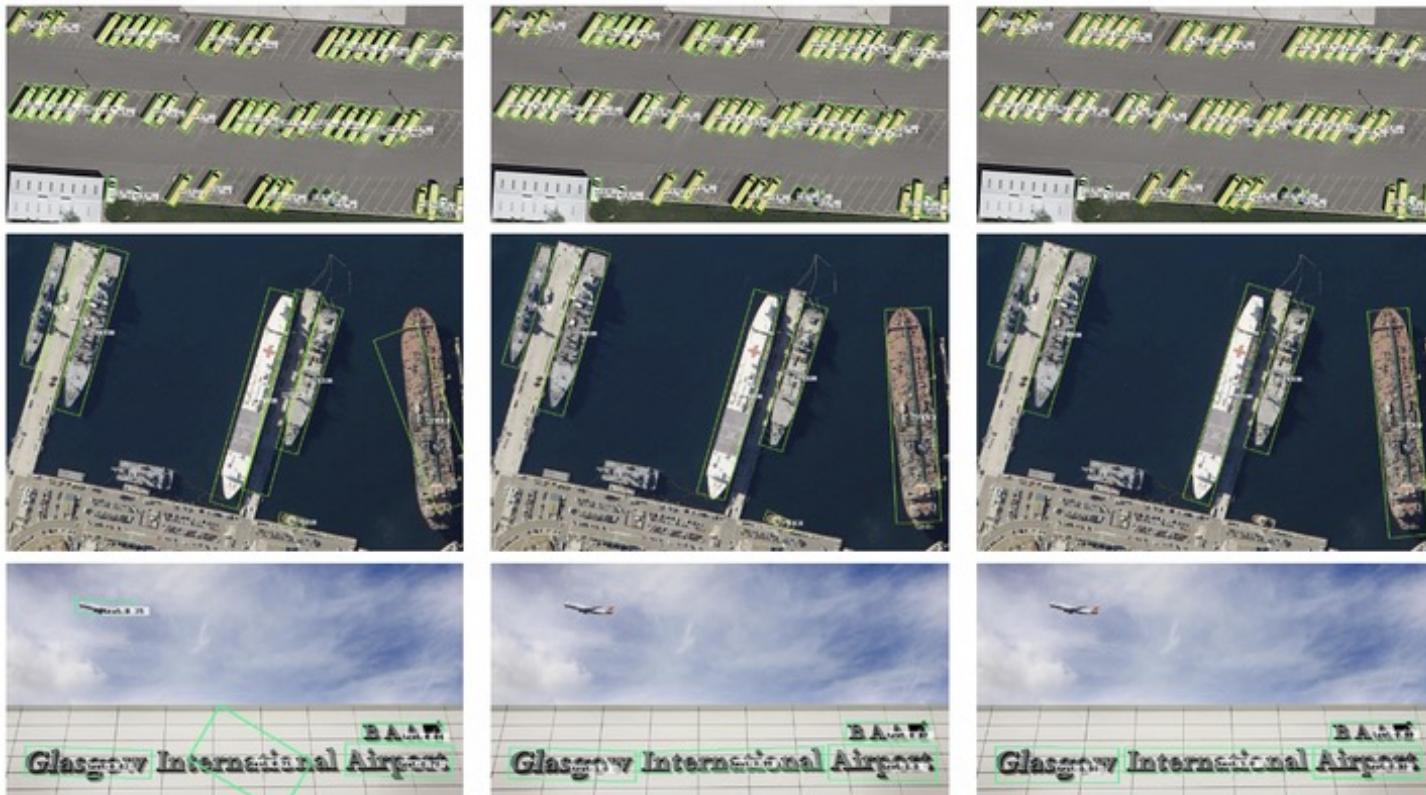




# 解决方法



- 高精度分析 (KLD>GWD>smooth L1) :





# 解决方法

- 尺度不变性比较

- 很明显GWD和 $L_2$ 不具有尺度不变性。
- 对于两个已知的高斯分布  $\mathbf{X}_p \sim \mathcal{N}_p(\boldsymbol{\mu}_p, \boldsymbol{\Sigma}_p)$  和  $\mathbf{X}_t \sim \mathcal{N}_t(\boldsymbol{\mu}_t, \boldsymbol{\Sigma}_t)$  假设有一个满秩的矩阵  $\mathbf{M}$  ( $|\mathbf{M}| \neq 0$ )，有：

$$\mathbf{X}_{p'} = \mathbf{M}\mathbf{X}_p \sim \mathcal{N}_p(\mathbf{M}\boldsymbol{\mu}_p, \mathbf{M}\boldsymbol{\Sigma}_p\mathbf{M}^\top), \mathbf{X}_{t'} = \mathbf{M}\mathbf{X}_t \sim \mathcal{N}_t(\mathbf{M}\boldsymbol{\mu}_t, \mathbf{M}\boldsymbol{\Sigma}_t\mathbf{M}^\top)$$

- 我们将其分别标记为  $\mathcal{N}_{p'}$  和  $\mathcal{N}_{t'}$ ，那么它们的KLD计算如下：

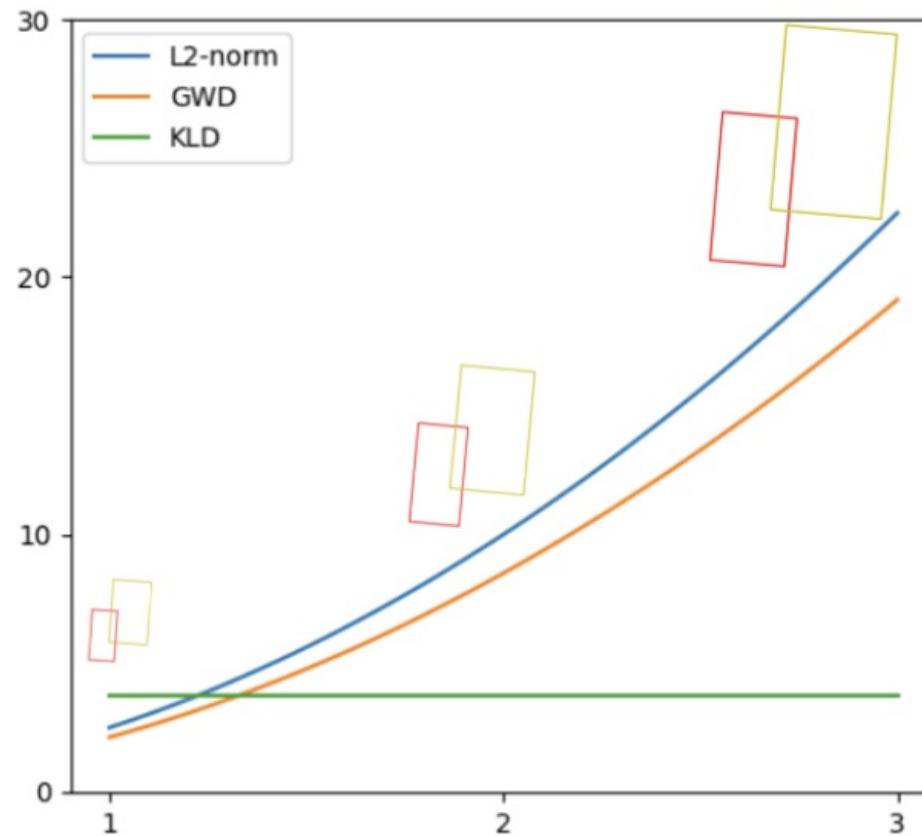
$$\begin{aligned} \mathbf{D}_{kl}(\mathcal{N}_{p'} || \mathcal{N}_{t'}) &= \frac{1}{2}(\boldsymbol{\mu}_p - \boldsymbol{\mu}_t)^\top \mathbf{M}^\top (\mathbf{M}^\top)^{-1} \boldsymbol{\Sigma}_t^{-1} \mathbf{M}^{-1} \mathbf{M} (\boldsymbol{\mu}_p - \boldsymbol{\mu}_t) \\ &\quad + \frac{1}{2} \mathbf{Tr}((\mathbf{M}^\top)^{-1} \boldsymbol{\Sigma}_t^{-1} \mathbf{M}^{-1} \mathbf{M} \boldsymbol{\Sigma}_p \mathbf{M}^\top) + \frac{1}{2} \ln \frac{|\mathbf{M}| |\boldsymbol{\Sigma}_t| |\mathbf{M}^\top|}{|\mathbf{M}| |\boldsymbol{\Sigma}_p| |\mathbf{M}^\top|} - 1 \\ &= \frac{1}{2}(\boldsymbol{\mu}_p - \boldsymbol{\mu}_t)^\top \boldsymbol{\Sigma}_t^{-1} (\boldsymbol{\mu}_p - \boldsymbol{\mu}_t) + \frac{1}{2} \mathbf{Tr}(\mathbf{M}^\top (\mathbf{M}^\top)^{-1} \boldsymbol{\Sigma}_t^{-1} \mathbf{M}^{-1} \mathbf{M} \boldsymbol{\Sigma}_p) + \frac{1}{2} \ln \frac{|\boldsymbol{\Sigma}_t|}{|\boldsymbol{\Sigma}_p|} - 1 \\ &= \mathbf{D}_{kl}(\mathcal{N}_p || \mathcal{N}_t) \end{aligned}$$

- 因此KLD具有仿射不变性的。当  $\mathbf{M} = k\mathbf{I}$  时，KLD的尺度不变性就被证明了。



# 解决方法

- 尺度不变性比较



1

## 旋转目标检测

2

## 问题和挑战

3

## 解决办法

4

## 实验分析





# 实验分析

- 在3种数据集和2种检测器上进行了高精度检测实验，KLD具有绝对优势。

Table 3: High-precision detection experiment under different regression loss. ‘R’, ‘F’ and ‘G’ indicate random rotation, flipping, and graying, respectively.

Method	Dataset	Data Aug.	Reg. Loss	Hmean <sub>50</sub> /AP <sub>50</sub>	Hmean <sub>60</sub> /AP <sub>60</sub>	Hmean <sub>75</sub> /AP <sub>75</sub>	Hmean <sub>85</sub> /AP <sub>85</sub>	Hmean <sub>50:95</sub> /AP <sub>50:95</sub>
RetinaNet	HRSC2016	R+F+G	Smooth L1	84.28	74.74	48.42	12.56	47.76
			GWD	85.56 (+1.28)	84.04 (+9.30)	60.31 (+11.89)	17.14 (+4.58)	52.89 (+5.13)
			KLD	87.45 (+3.17)	86.72 (+11.98)	72.39 (+23.97)	27.68 (+15.12)	57.80 (+10.04)
R <sup>3</sup> Det	MSRA-TD500	R+F+G	Smooth L1	88.52	79.01	43.42	4.58	46.18
			GWD	89.43 (+0.91)	88.89 (+9.88)	65.88 (+22.46)	15.02 (+10.44)	56.07 (+9.89)
			KLD	89.97 (+1.45)	89.73 (+10.72)	77.38 (+33.96)	25.12 (+20.54)	61.40 (+15.22)
RetinaNet	MSRA-TD500	R+F+G	Smooth L1	70.98	62.42	36.73	12.56	37.89
			GWD	76.76 (+5.78)	68.58 (+6.16)	44.21 (+7.48)	17.75 (+5.19)	43.62 (+5.73)
			KLD	76.96 (+5.98)	70.08 (+7.66)	46.95 (+10.22)	19.59 (+7.03)	45.24 (+7.35)
R <sup>3</sup> Det	ICDAR2015	F	Smooth L1	69.78	64.15	36.97	8.71	37.73
			GWD	74.29 (+4.51)	68.34 (+4.19)	43.39 (+6.42)	10.50 (+1.79)	41.68 (+3.95)
			KLD	75.32 (+5.54)	69.94 (+5.79)	44.46 (+7.49)	10.70 (+1.99)	42.68 (+4.95)
RetinaNet	ICDAR2015	R+F	Smooth L1	74.83	69.46	42.02	11.59	41.98
			GWD	76.15 (+1.32)	71.26 (+1.80)	45.59 (+3.57)	11.65 (+0.06)	43.58 (+1.60)
			KLD	77.92 (+3.09)	72.77 (+3.31)	43.27 (+1.25)	11.09 (-0.50)	43.65 (+1.67)
R <sup>3</sup> Det	ICDAR2015	F	Smooth L1	74.28	68.12	35.73	8.01	39.10
			GWD	75.59 (+1.31)	68.36 (+0.24)	40.24 (+4.51)	9.15 (+1.14)	40.80 (+1.70)
			KLD	77.72 (+2.43)	71.99 (+3.87)	43.95 (+8.22)	10.43 (+2.42)	43.29 (+4.19)
R <sup>3</sup> Det	ICDAR2015	R+F	Smooth L1	75.53	69.69	37.69	9.03	40.56
			GWD	77.09 (+1.56)	71.52 (+1.83)	41.08 (+3.39)	10.10 (+1.07)	42.17 (+1.61)
			KLD	79.63 (+4.63)	73.30 (+3.61)	43.51 (+5.82)	10.61 (+1.58)	43.61 (+3.05)



# 实验分析

- 我们在一些更具有挑战性的数据集上进行了验证实验，包括DOTA-v1.5和DOTA-v2.0（包含很多像素值小于10的目标），KLD依旧表现出色。

Table 5: Accuracy comparison between different rotation detectors on DOTA dataset.  $\dagger$  and  $\ddagger$  represent the large aspect ratio object and the square-like object, respectively. The bold red and blue fonts indicate the top two performances respectively.  $D_{oc}$  and  $D_{le}$  represent OpenCV Definition ( $\theta \in [-90^\circ, 0^\circ]$ ) and Long Edge Definition ( $\theta \in [-90^\circ, 90^\circ]$ ) of RBox.

Baseline	Method	Box Def.	v1.0 trainval/test								v1.0 train/val			v1.5	v2.0	
			BR $\dagger$	SV $\dagger$	LV $\dagger$	SH $\dagger$	HA $\dagger$	ST $\dagger$	RA $\dagger$	7-AP <sub>50</sub>	AP <sub>50</sub>	AP <sub>75</sub>	AP <sub>50:95</sub>	AP <sub>50</sub>	AP <sub>50</sub>	
RetinaNet	-	$D_{oc}$	42.17	65.93	51.11	72.61	53.24	78.38	62.00	60.78	65.73	64.70	32.31	34.50	58.87	44.16
	-	$D_{le}$	38.31	60.48	49.77	68.29	51.28	78.60	60.02	58.11	64.17	62.21	26.06	31.49	56.10	43.06
	IoU-Smooth L1 [3]	$D_{oc}$	44.32	63.03	51.25	72.78	56.21	77.98	63.22	61.26	66.99	64.61	34.17	36.23	59.16	46.31
	Modulated Loss [43]	$D_{oc}$	42.92	67.92	52.91	72.67	53.64	<b>80.22</b>	58.21	61.21	66.05	63.50	33.32	34.61	57.75	45.17
	Modulated Loss [43]	Quad.	43.21	70.78	54.70	72.68	<b>60.99</b>	79.72	62.08	63.45	67.20	65.15	40.59	<b>39.12</b>	<b>61.42</b>	<b>46.71</b>
	RIL [32]	Quad.	40.81	67.63	55.45	72.42	55.49	78.09	64.75	62.09	66.06	64.07	<b>40.98</b>	39.05	58.91	45.35
	CSL [4]	$D_{le}$	42.25	68.28	54.51	72.85	53.10	75.59	58.99	60.80	67.38	64.40	32.58	35.04	58.55	43.34
	DCL (BCL) [44]	$D_{le}$	41.40	65.82	56.27	73.80	54.30	79.02	60.25	61.55	67.39	<b>65.93</b>	35.66	36.71	59.38	45.46
	GWD [5]	$D_{oc}$	<b>44.07</b>	<b>71.92</b>	<b>62.56</b>	<b>77.94</b>	60.25	79.64	<b>63.52</b>	<b>65.70</b>	<b>68.93</b>	65.44	38.68	38.71	60.03	46.65
	KLD	$D_{oc}$	<b>44.00</b>	<b>74.45</b>	<b>72.48</b>	<b>84.30</b>	<b>65.54</b>	<b>80.03</b>	<b>65.05</b>	<b>69.41</b>	<b>71.28</b>	<b>68.14</b>	<b>44.48</b>	<b>42.15</b>	<b>62.50</b>	<b>47.69</b>
R <sup>3</sup> Det [26]	-	$D_{oc}$	44.15	75.09	72.88	86.04	56.49	82.53	61.01	68.31	70.66	67.18	38.41	38.46	62.91	48.43
	DCL (BCL) [44]	$D_{le}$	<b>46.84</b>	74.87	74.96	85.70	57.72	<b>84.06</b>	<b>63.77</b>	69.70	71.21	67.45	35.44	37.54	61.98	48.71
	GWD [5]	$D_{oc}$	46.73	<b>75.84</b>	<b>78.00</b>	<b>86.71</b>	<b>62.69</b>	<b>83.09</b>	61.12	<b>70.60</b>	<b>71.56</b>	<b>69.28</b>	<b>43.35</b>	<b>41.56</b>	<b>63.22</b>	<b>49.25</b>
	KLD	$D_{oc}$	<b>48.34</b>	<b>75.09</b>	<b>78.88</b>	<b>86.52</b>	<b>65.48</b>	82.08	<b>61.51</b>	<b>71.13</b>	<b>71.73</b>	<b>68.87</b>	<b>44.48</b>	<b>42.11</b>	<b>65.18</b>	<b>50.90</b>



# 实验分析

- 在水平检测任务上（COCO数据集），KLD也是和GIoU等常见损失函数保持差不多的水平。

Table 6: Performance evaluation of KLD on classic horizontal detection.

Detector	Reg. Loss	AP	AP <sub>50</sub>	AP <sub>75</sub>	AP <sub>s</sub>	AP <sub>m</sub>	AP <sub>l</sub>	Detector	Reg. Loss	AP	AP <sub>50</sub>	AP <sub>75</sub>	AP <sub>s</sub>	AP <sub>m</sub>	AP <sub>l</sub>
RetinaNet	Smooth L1	37.2	56.6	39.7	21.4	41.1	48.0	Faster RCNN	Smooth L1	37.9	58.8	41.0	22.4	41.4	49.1
	GIoU	37.4	56.7	39.7	22.2	41.7	48.1		GIoU	<b>38.3</b>	58.7	41.5	22.5	41.7	49.7
	KLD	<b>38.0</b>	56.4	40.6	23.3	43.2	49.3		KLD	38.2	58.7	41.7	22.6	41.8	49.3

- 我们对KLD不同变体在两个数据集上进行了实验，发现最后的效果是差不多的，排除了不对称性对结果的干扰。

Table 2: Ablation of different KLD-based regression loss form. The based detector is RetinaNet.

Dataset	D <sub>kl</sub> (N <sub>p</sub>   N <sub>t</sub> )	D <sub>kl</sub> (N <sub>t</sub>   N <sub>p</sub> )	D <sub>kl_min</sub> (N <sub>p</sub>   N <sub>t</sub> )	D <sub>kl_max</sub> (N <sub>p</sub>   N <sub>t</sub> )	D <sub>js</sub> (N <sub>p</sub>   N <sub>t</sub> )	D <sub>jeffreys</sub> (N <sub>p</sub>   N <sub>t</sub> )
DOTA-v1.0	70.17	70.64	<b>70.71</b>	70.55	69.67	70.56
HRSC2016	82.83	83.82	83.60	82.70	<b>84.06</b>	83.66

# 实验分析



- 最后在DOTA-v1.0的SOTA实验中，我们也取得了当前所发表论文里的最高性能。

Table 7: AP on different objects on DOTA-v1.0. Here R-101 denotes ResNet-101 (likewise for R-50, R-152), and RX-101 and H-104 represent ResNeXt101 [46] and Hourglass-104 [47], respectively. MS indicates that multi-scale training/testing is used. **Red** and **blue** indicate the top two performances.

	Method	Backbone	MS	PL	BD	BR	GTF	SV	LV	SH	TC	BC	ST	SBF	RA	HA	SP	HC	AP <sub>50</sub>
Two-stage	ICN [29]	R-101	✓	81.40	74.30	47.70	70.30	64.90	67.80	70.00	90.80	79.10	78.20	53.60	62.90	67.00	64.20	50.20	68.20
	RoI-Trans. [11]	R-101	✓	88.64	78.52	43.44	75.92	68.81	73.68	83.59	90.74	77.27	81.46	58.39	53.54	62.83	58.93	47.67	69.56
	SCRDet [3]	R-101	✓	89.98	80.65	52.09	68.36	68.36	60.32	72.41	90.85	<b>87.94</b>	86.86	65.02	66.68	66.25	68.24	65.21	72.61
	Gliding Vertex [48]	R-101		89.64	85.00	52.26	77.34	73.01	73.14	86.82	90.74	79.02	86.81	59.55	<b>70.91</b>	72.94	70.86	57.32	75.02
	Mask OBB [49]	RX-101	✓	89.56	85.95	54.21	79.90	76.52	74.16	85.63	89.85	83.81	86.48	54.89	69.64	73.94	69.06	63.32	75.33
	CenterMap OBB [50]	R-101	✓	89.83	84.41	54.60	70.25	77.66	78.32	87.19	90.66	84.89	85.27	56.46	69.23	74.13	71.56	66.06	76.03
	FPN-CSL [4]	R-152	✓	<b>90.25</b>	<b>85.53</b>	54.64	75.31	70.44	73.51	77.62	90.84	86.15	86.69	69.60	68.04	73.83	71.10	68.93	76.17
	RSDet-II [43]	R-152	✓	89.93	84.45	53.77	74.35	71.52	78.31	78.12	<b>91.14</b>	87.35	86.93	65.64	65.17	75.35	<b>79.74</b>	63.31	76.34
	SCRDet++ [51]	R-101	✓	<b>90.05</b>	84.39	55.44	73.99	77.54	71.11	86.05	90.67	87.32	87.08	69.62	68.90	73.74	71.29	65.08	76.81
Single-stage	ReDet [52]	ReR-50	✓	88.81	82.48	<b>60.83</b>	80.82	78.34	<b>86.06</b>	88.31	90.87	<b>88.77</b>	87.03	68.65	66.90	<b>79.26</b>	<b>79.71</b>	74.67	80.10
	PIoU [30]	DLA-34 [53]		80.90	69.70	24.10	60.20	38.30	64.40	64.80	<b>90.90</b>	77.20	70.40	46.50	37.10	57.10	61.9	64.00	60.50
	O <sup>2</sup> -DNet [54]	H-104	✓	89.31	82.14	47.33	61.21	71.32	74.03	78.62	90.76	82.23	81.36	60.93	60.17	58.21	66.98	61.03	71.04
	DAL [14]	R-101	✓	88.61	79.69	46.27	70.37	65.89	76.10	78.53	90.84	79.98	78.41	58.71	62.02	69.23	71.32	60.65	71.78
	P-RSDet [55]	R-101	✓	88.58	77.83	50.44	69.29	71.10	75.79	78.66	90.88	80.10	81.71	57.92	63.03	66.30	69.77	63.13	72.30
	BBAVectors [56]	R-101	✓	88.35	79.96	50.69	62.18	78.43	78.98	87.94	90.85	83.58	84.35	54.13	60.24	65.22	64.28	55.70	72.32
	DRN [13]	H-104	✓	89.71	82.34	47.22	64.10	76.22	74.43	85.84	90.57	86.18	84.89	57.65	61.93	69.30	69.63	58.48	73.23
	PolarDet [57]	R-101	✓	89.65	<b>87.07</b>	48.14	70.97	78.53	80.34	87.45	90.76	85.63	86.87	61.64	70.32	71.92	73.09	67.15	76.64
	RDD [58]	R-101	✓	89.15	83.92	52.51	73.06	77.81	79.00	87.08	90.62	86.72	87.15	63.96	70.29	76.98	75.79	72.15	77.75
Refine-stage	GWD [5]	R-152	✓	89.06	84.32	55.33	77.53	76.95	70.28	83.95	89.75	84.51	86.06	<b>73.47</b>	67.77	72.60	75.76	74.17	77.43
	KLD	R-50		88.91	83.71	50.10	68.75	78.20	76.05	84.58	89.41	86.15	85.28	63.15	60.90	75.06	71.51	67.45	75.28
		R-50	✓	88.91	85.23	53.64	81.23	78.20	76.99	84.58	89.50	86.84	86.38	71.69	68.06	75.95	72.23	75.42	78.32
	CFC-Net [31]	R-101	✓	89.08	80.41	52.41	70.02	76.28	78.11	87.21	90.89	84.47	85.64	60.51	61.52	67.82	68.02	50.09	73.50
	R'Det [26]	R-152	✓	89.80	83.77	48.11	66.77	78.76	83.27	87.84	90.82	85.38	85.51	65.67	62.68	67.53	78.56	72.62	76.47
	DAL [14]	R-50	✓	89.69	83.11	55.03	71.00	78.30	81.90	88.46	90.89	84.97	<b>87.46</b>	64.41	65.65	76.86	72.09	64.35	76.95
	DCL [44]	R-152	✓	89.26	83.60	53.54	72.76	79.04	82.56	87.31	90.67	86.59	86.98	67.49	66.88	73.29	70.56	69.99	77.37
	RIDet [32]	R-50	✓	89.31	80.77	54.07	76.38	<b>79.81</b>	81.99	<b>89.13</b>	90.72	83.58	87.22	64.42	67.56	78.08	79.17	62.07	77.62
	S <sup>2</sup> A-Net [12]	R-101	✓	89.28	84.11	56.95	79.21	<b>80.18</b>	82.93	<b>89.21</b>	90.86	84.66	<b>87.61</b>	71.66	68.23	<b>78.58</b>	78.20	65.55	79.15
Refine-stage	R <sup>3</sup> Det-GWD [5]	R-152	✓	89.66	84.99	<b>59.26</b>	<b>82.19</b>	78.97	<b>84.83</b>	87.70	90.21	86.54	86.85	<b>73.04</b>	67.56	76.92	79.22	74.92	<b>80.19</b>
		R-50		88.90	84.17	55.80	69.35	78.72	84.08	87.00	89.75	84.32	85.73	64.74	61.80	76.62	78.49	70.89	77.36
	R <sup>3</sup> Det-KLD	R-50	✓	89.90	84.91	59.21	78.74	78.82	83.95	87.41	89.89	86.63	86.69	70.47	70.87	76.96	79.40	<b>78.62</b>	80.17
		R-152	✓	89.92	85.13	59.19	<b>81.33</b>	78.82	84.38	87.50	89.80	87.33	87.00	72.57	<b>71.35</b>	77.12	79.34	<b>78.68</b>	<b>80.63</b>

# 谢谢！

